



SpeedLabs
MATHS

ICSE 8th

TEEVRA EDUTECH PVT. LTD.

INEQUALITIES

1. If $x \in \{-3, -2, -1, 0, 1, 2, 3\}$, find the solution set of each of the following:

(i) $x + 2 < 1$

Ans. $x + 2 < 1$

$$\Rightarrow x \leq -1$$

Therefore, Solution Set = $\{-3, -2\}$

(ii) $3 - 5x < -1$

Ans. $3 - 5x < -1$

$$\Rightarrow 5x > 4$$

$$\Rightarrow x > 4/5$$

Therefore, Solution Set = $\{1, 2, 3\}$

2. If $x \in N$; find the solution set of each of the following in equation: $N = \{1, 2, 3, \dots\}$

(i) $3x - 8 < 0$

$$\Rightarrow 3x < 8$$

$$\Rightarrow x < \frac{8}{3}$$

Solution Set = $\{1, 2\}$

(ii) $\frac{-1}{4} \leq \frac{1}{2} - \frac{2}{3}$

Ans. $\frac{-1}{4} \leq \frac{1}{2} - \frac{2}{3}$

$$\Rightarrow \frac{-3}{4} \leq \frac{-x}{3}$$

$$\Rightarrow \frac{x}{3} \leq \frac{3}{4}$$

$$\Rightarrow x \leq \frac{9}{4}$$

Solution Set = $\{1, 2\}$

3. If $x \in \mathbb{Z}$, find the solution set of the following in equations: $\mathbb{Z} = \{-3, -2, -1, 0, 1, 2, 3, \dots\}$

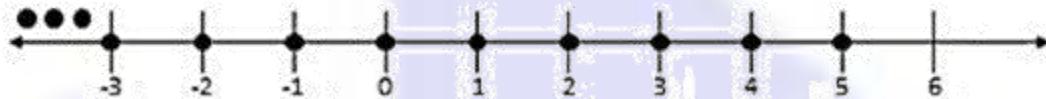
(i) $9x - 7 \leq 25 + 3x$

Ans. $9x - 7 \leq 25 + 3x$

$$\Rightarrow 6x \leq 32$$

$$\Rightarrow x \leq \frac{32}{6}$$

$$\text{Solution Set} = \{-3, -2, -1, 0, 1, 2, 3, 4, 5, \dots\}$$



(ii) $10 - 2(1 + 4x) < 20$

Ans. $10 - 2(1 + 4x) < 20$

$$\Rightarrow 10 - 2 - 20 < 8x$$

$$\Rightarrow 8x > -12$$

$$\Rightarrow x > -\frac{3}{2}$$

$$\text{Solution set} = \{-1, 0, 1, 2, \dots\}$$



4. Find the Solution Set of each of the following in equations and represent the solution on a real line.

(i) $1 - 4x \geq -1, x \in \mathbb{N}$

Ans. $1 - 4x \geq -1, x \in \mathbb{N}$

$$\Rightarrow 4x \leq 2$$

$$\Rightarrow x \leq \frac{1}{2}$$

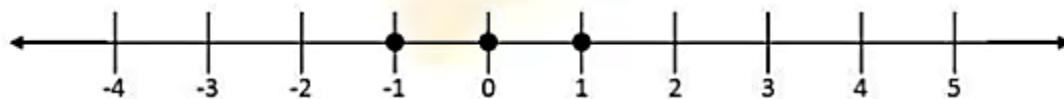
$$\text{Solution Set} = \emptyset$$

(ii) $-3 \leq 4x + 1 < 9, x \in \mathbb{N}$

$$\Rightarrow -4 \leq 4x < 8$$

$$\Rightarrow -1 \leq x < 2$$

$$\text{Solution set} = \{-1, 0, 1\}$$



(iii) $3 + \frac{x}{4} < \frac{2x}{3} + 5, x \in \mathbb{R}$

Ans. $3 + \frac{x}{4} < \frac{2x}{3} + 5, x \in \mathbb{R}$

$$\Rightarrow \frac{x}{4} < \frac{2x}{3} + 2$$

$$\Rightarrow \frac{2x}{3} - \frac{x}{4} > -2$$

$$\Rightarrow 5x > -24$$

$$\Rightarrow x > \frac{(-24)}{5}$$

Solution Set = $\{x \in \mathbb{R} : x > \frac{(-24)}{5}\}$



(iv) $\frac{1}{3}(4x - 1) + 3 \leq 4 + \frac{2}{5}(6x + 2) + \frac{4}{5}$

Ans. $\frac{1}{3}(4x - 1) + 3 \leq 4 + \frac{2}{5}(6x + 2) + \frac{4}{5}$

$$\Rightarrow \frac{4}{3}x - \frac{1}{3} + 3 \leq 4 + \frac{12}{5}x + \frac{4}{5}$$

$$\Rightarrow \frac{(-32)}{15} \leq \frac{16}{15}x$$

$$\Rightarrow x \geq -2$$

Solution Set = $\{x \in \mathbb{R} : x \geq -2\}$

